

2021 Secondary 4 Mathematics Prelim Paper 2 Marking Scheme

No.	Solution	Mark	Remarks
1ai	$\frac{w^2}{3}$	B1	
1aii	$\frac{3}{y-1} - \frac{5}{y+6}$ $= \frac{3y+18-5y+5}{(y-1)(y+6)}$ $= \frac{-2y+23}{(y-1)(y+6)}$	M1 A1	Combine fraction
1aiii	$\frac{2v^2 - 5v - 12}{16 - v^2}$ $= \frac{(2v+3)(v-4)}{(4+v)(4-v)}$ $= -\frac{2v+3}{v+4}$	M1 B1 A1	Factorise numerator (4 + v)(4 - v) seen o.e
			Total: 6 marks
2a	$\begin{pmatrix} 50 & 40 \\ 0 & 20 \\ 20 & 30 \end{pmatrix}$	B1	cao
2b	$\begin{pmatrix} 111 & 140 \\ 8 & -1 \end{pmatrix}$	B1 B1	-1 for each error
2c	<u>Stall A</u> because he would pay \$8 more in stall B	B1	
2d	$[(111+8) + (140 - 1)] \times 0.7$ $= 83.3 + 97.3$ $= \$180.60$	B1 M1 A1	119 or 139 seen $\times 0.7$ 2 d.p
			Total: 7 marks
3ai	$\text{Height} = \frac{52.6}{12.7}$ $= 4.1417$ $\sin 50 = \frac{4.1417}{RS}$ $RS = 5.4066$ $= 5.407 \text{ (shown)}$	B1 B1	Height = $QR \sin 130$ 5.4066
3aii	$QS^2 = 12.7^2 + 5.407^2 - 2(12.7)(5.407) \cos 130$ $QS = 16.7$	M1 A1	Apply Cosine rule, $\cos 130$
3bi	$\angle ABC = 180 - 118 \text{ (}\angle\text{s in opposite segment)}$ $= 62$	B1	with reason
3bii	$\text{reflex } \angle AOC = 236 \text{ (}\angle \text{ at centre} = 2\angle \text{ at circumference)}$ $\angle BCO = 360 - 32 - 236 - 62$ $= 30$	B1 B1	
			Total: 7 marks

No.	Solution	Mark	Remarks
4a	$OP = OQ$ (equal chords; $AB = BC$) $\angle OPA = \angle OQC = 90$ (perpendicular bisector of chord) $AO = OC$ (radii of circle) Triangle $OAP \equiv$ triangle OCQ (RHS) Alternatively, $AP = CQ$ ($AB = BC$, $AP = \frac{1}{2} AB$, $CQ = \frac{1}{2} BC$) $OP = OQ$ (equal chords; $AB = BC$) $AO = OC$ (radii of circle) Triangle $OAP \equiv$ triangle OCQ (SSS)	B1 B1 B1 B1 B1 B1	-1 for test not stated
4b	Shaded area = $2 \times$ $\left[\frac{1}{2}(6)^2 \left(\frac{11\pi}{18} \right) - \frac{1}{2}(6)^2 \sin \frac{11\pi}{18} \right]$ $= 35.3$ Alternatively, Shaded area = $\pi(6)^2 - \left(2 \times \frac{1}{2}(6)^2 \sin \frac{11\pi}{18} \right) - \frac{1}{2}(6)^2 \frac{7\pi}{9}$	B1 M1 M1 A1	$\frac{11\pi}{18}$ seen Area of sector Area of triangle
			Total: 7 marks
5a	greatest possible area = $\frac{250.5}{8.35}$ $= 30$	B1 B1	250.5 seen cao
5bi	$\angle RAB = \angle QPB$ (corresponding \angle) $\angle ARB = \angle PQB$ (corresponding \angle) $\angle RCA$ is shared/common Triangles ABR and PBQ are similar (AA)	B1 B1	
5bii	Area PBQ : Area of Trapezium $= 25 : 36 - 25$ $= 25 : 11$	B1 AG	36 - 25 seen
5biii	Area of $ABR = \frac{22}{11} \times 36 = 72$ Area of $ABC = \frac{72}{3} \times 5$ $= 120$	B1 M1 A1	72 soi $\frac{\text{Their area } ABR}{3} \times 5$
			Total: 8 marks

6ai	50 900	B1	50 893.8 50 900.4
6aii	$h = \frac{25893.8}{\pi(18)^2}$ $= 25.4$	M1 A1	
6aiii	Number of cups = $\frac{25000}{\frac{2}{3}\pi(3.5)^3}$ = 278	M1 A1	Volume of hemp cao
6b	Surface area = $6x(6x) \times 5 + \frac{1}{2}(5x)(6x) \times 4$ = $240x^2$	M1 B1 M1 A1	$6x6x$ (area of sq) Slant $h = 5x$ $\frac{1}{2}$ (Their slant height)($6x$) $\times 4$ cao
Total: 9 marks			
7a	$P = 2x + \left(\frac{60}{x}\right) \times 2$ $= 2x + \frac{120}{x}$	B1	$\left(\frac{60}{x}\right) \times 2$ seen
7b	64	B1	
7c		P2 C1	-1 mark for every wrong point plotted
7d	$4.7 \leq x \leq 12.9$	B1 B1	4.6 to 4.8 and 12.8 to 13.0 $4.68 \leq x \leq 12.82$
7e	$p = 4x$	B1	
Total: 8 marks			

8a	$p = 121876.00$ $q = 21818.00$	B1 B1	Accept $p = 121876$ $q = 21818$
8bi	$3350 + 0.115 (100058 - 80000)$ $= \$5656.67$ (shown)	B1 B1	3350 seen 20058 soi
8bii	<p>Angie's income tax = 0.55×5656.67 = \$3111.1685</p> <p>Let x be the remaining income. $550 + x (7\%) = 3111.1685$ $x = \\$36588.1214$ Angie's chargeable income $= 40\,000 + 36588.1214$ $= \\$76588.12$</p> <p>$\frac{76588.12}{100058} \times 100\% = 76.5\%$</p> <p>Disagree as Angie's is 0.44 times Ahmad's chargeable income.</p> <p>or $100058 \times 55\% = \\$55\,031.90$ Disagree as Angie's income is less than \$55 031.90.</p>	M1 M1 B1 A1 A1 A1	<p>Finding Angie's income tax</p> <p>Formulate 550 or 40000 seen \$76588.12</p> <p>Express Angie's income as percentage</p> <p>Finding what 55% of Ahmad's income is</p>
			Total: 9 marks

9a	25 21	B1 B1	
9b	1025 isn't a perfect square	B1	oe
9c	$1584 = 561 + n^2 - 1$ $n^2 = 1024$ $n = 32$	M1 A1	
9di	$R = \frac{3}{2}n(n+1)$	B1	oe
9dii	408	B1	
9e	$D = \frac{1}{2}(n+1)(n+2)$	B1	oe
			Total: 8 marks
10a	121, 127.5, 132 120 and 131	B1 B1 B1	<i>LQ UQ</i> Median <i>LQ UQ</i>
10b	The median of the cumulative curve will be on the left.	B1	
10ci	<u>False because the median mass for apples is lower.</u>	B1	
10cii	<u>True because upper quartile for mass of oranges is higher</u>	B1	
10di	126.25 or $126\frac{1}{4}$	B1	Accept 3s.f and above (126, ...)
10dii	8.57	B1	cao
10diii	$1 - \frac{15}{40} \times \frac{14}{39}$ $= \frac{45}{52}$ Or $\frac{25}{40} \times \frac{24}{39} + \frac{25}{40} \times \frac{15}{39} \times 2$ $= \frac{45}{52}$	M1 A1 M1 A1	When all weight less than 125g
			Total: 10 marks
11ai	$\frac{72}{x}$	B1	
11aai	$\frac{144}{x-2}$	B1	
11aiii	$\frac{72}{x} + \frac{144}{x-2} = 25$ $72(x-2) + 144x = 25(x-2)$ $216x - 144 = 25x^2 - 50x$	B1 B1	Their ai + aii = 25

	$25x^2 - 266x + 144 = 0$ (shown)		
11aiv	$x = \frac{22 \pm \sqrt{266^2 - 4(25)(144)}}{2(25)}$ $x = 10.068 \text{ or } 0.572$	M1	
11b	$\text{Time} = \frac{4}{10.068 - 2}$ $= 29 \text{ mins } 45 \text{ secs}$	M1 A1	Ignore rejection Replace 11aiv by $x = 10.068$
			Total: 9 marks
12ai 12aia 12aiii		B1 B1 B1	
12b	<p>D because the psf is the lowest</p> <p>Or D because price per metre square is the lowest.</p>	B1	
12c	<p>John and Chieh</p> $\text{Purchase price} = 46\,500 - 80\,000 - 50\,000$ $= 46\,500 - 130\,000$ $= \$335\,000$ $\text{Interest} = (\text{their purchase price}) \times 0.9 \times 2.6\% \times 15$ $= \$117\,585$ <p>Janet</p> $\text{Purchase price} = 348\,338 - 50\,000 - 15\,000^*$ $= 283\,338$ $(\text{their purchase price}) \times 0.75 \times 1.8\% \times n < 117585$ $n < 30.7$ <p>Janet should finish servicing her loan in 20 years to incur less interest. I took the average of the grant for PHG as I am unsure if she would receive the full grant or not.</p>	B1 M1 B1 M1 M1 B1 B1	<p>[choosing C]</p> <p>46 500 seen</p> <p>Find purchase price – grant</p> <p>130 000 seen</p> <p>Find Int. (HDB)</p> <p>*10000 – 20000</p> <p>Find Int. (Bank)</p> <p>State the no of years.</p> <p>State assumption</p>
			Total: 12 marks